## CHAPMAN-JOUGUET PRESSURE FOR EXPLOSIVES

one obtains

$$p_m/P_x = \left[\rho_m^0 D_m / \rho_x^0 D_x\right] \times \left[(\rho_x^0 D_x + \rho_r^0 D_r) / (\rho_m^0 D_m + \rho_r^0 D_r)\right].$$
(2)

If one makes the acoustic approximation  $\rho_r^0 D_r = \rho_x^0 D_x$ , Eq. (2) simplifies to

$$P_{x} = (P_{m}/2\rho_{m}^{0}D_{m})(\rho_{x}^{0}D_{x} + \rho_{m}^{0}D_{m}).$$
(3)

Error analysis shows  $P_x$  to be quite insensitive to error in  $\rho_r^0 D_r$ ; for example, in Composition B a 10% error in  $\rho_r^0 D_r$  corresponds only to a 1% error in  $P_x$ . A more precise treatment of the interface interaction by W. Fickett and R. D. Cowan<sup>7</sup> gives for the cases of interest in this paper values of explosive pressure only about 1% higher than those resulting from the acoustic approximation.

If in Eq. (3) one identifies  $P_m$  as  $P_m^*$  and  $P_x$  as the C-J pressure  $(P_{cj})$  of the explosive, then  $P_{cj}$  can be established since  $\rho_x^0$  and  $\rho_m^0$  are the simply measurable initial densities of the explosive and the inert,  $D_x$  is the



PH. UW)

Fig. 3. Interaction at the interface between explosive and inert material in contact with it. M is the inert material Hugoniot; the X's are Hugoniots for the reacted products of the explosive.

readily measurable detonation velocity<sup>8</sup> and  $D_m^*$  and  $P_m^*$  are available from equation of state data if one hydrodynamic variable of this state is measured.<sup>9</sup> The quantity established in these experiments was the free-surface velocity  $(U_{fs}^*)$ .

An alternative method of establishing the C-J state, which minimizes the hitherto neglected effect of the reflected wave in the explosive on the reaction kinetics, is to establish the  $P_m^*$  state for each of several inert materials of different shock impedance. The state points define a curve in the pressure-particle velocity plane which closely approximates the locus of all possible shocked and rarefied states (for one direction of wave travel) from the C-J state of the explosive. It differs from this locus only insofar as the wave reflected back into the explosive affects the reaction kinetics; however, the amplitude of the reflected wave approaches zero as

<sup>7</sup> R. D. Cowan and W. Fickett, J. Chem. Phys. 24, 932 (1956).
<sup>8</sup> Campbell, Malin, Boyd, and Hull, Rev. Sci. Instr. 27, 567 (1956).
<sup>9</sup> Alsh, Rice, McQueen, and Yarger, Phys. Rev. (to be pub-



FIG. 4. Plexiglas block assembly for measurement of free-surface velocity of an explosive-driven plate.

one approaches the C-J state on this curve. The C-J state must also lie on the line  $P_{cj}/U_{cj} = \rho_x^{\ 0}D_x$  (where  $U_{cj}$  is the C-J particle velocity). The C-J point is thus established as the intersection of this line with the aforementioned curve at the point where the perturbation of the reaction by a reflected wave is minimized.

## EXPERIMENTAL TECHNIQUE

The value of free-surface velocity corresponding to  $P_m^*$  for a given explosive and inert material was determined by measurement of free-surface velocity of an explosive-driven plate as a function of plate thickness. These velocities were measured photographically by use of a rotating-mirror smear camera with a writing speed of 3.2 mm/µsec. A Plexiglas block assembly such as that of Figs. 4 and 5 was placed on the surface to be studied. This was viewed by the camera through a slit and swept on the film in a direction perpendicular to the slit image. When the explosive-driven plate on which such an assembly is placed begins to move, the argon gaps near the plate surface are closed first and yield a brilliant



Frg. 5. Disassembled parts of the plate assembly for a free-surface velocity record such as shown in Fig. 6.

797

SEPTEMBER, 1957

this reflected wave on

sequent change in the

gible in the following

ve travels through the

action overtakes and

e corresponding to the

hen in further travel

tion corresponding to

overtakes and reduces

ock front. Shock front

on of the thickness of

tatively as shown in

e-thickness curve may

on the pressure profile

particular, corresponds

1 the detonation wave.

at the explosive-inert

etonation wave,  $P_m$  is

material, and the  $\rho$ 's,

e velocities, and shock

ctively, particularized

he detonation wave, m

and r referring to the

Conditions in front of

superscript zero. All

the particle velocities

the momentum con-, and  $P_m = \rho_m^0 U_m D_m$ ,

ction of material thickness pressure corresponding to

lished).

(1)

c. 3, one can write

 $z - U_m),$ 

kness

'es'

ol have been

um plates in

he velocities. 89, 292, and